

Find the Limit.

$$(1) \lim_{(x,y) \rightarrow (2,1)} (x + 3y^2)$$

$$(2) \lim_{(x,y) \rightarrow (2,4)} \frac{x + y}{x - y}$$

$$(3) \lim_{(x,y) \rightarrow (0,1)} \frac{\arcsin(x/y)}{1 + xy}$$

$$(4) \lim_{(x,y) \rightarrow (0,0)} (5x + 3xy + y + 1)$$

$$(5) \lim_{(x,y) \rightarrow (0,0)} \ln(x^2 + y^2)$$

$$(6) \lim_{(x,y) \rightarrow (0,0)} \frac{\sin(x^2 + y^2)}{x^2 + y^2}$$

$$(7) \lim_{(x,y) \rightarrow (1,1)} \frac{x}{\sqrt{x+y}}$$

$$(8) \lim_{(x,y) \rightarrow (0,0)} e^{xy}$$

$$(9) \lim_{(x,y) \rightarrow (0,0)} \left(\frac{x^2}{(x^2 + 1)(y^2 + 1)} \right)$$

$$(10) \lim_{(x,y) \rightarrow (0,0)} \left[1 - \frac{\cos(x^2 + y^2)}{x^2 + y^2} \right]$$

Answer Key

(1) 5

(2) -3

(3) 0

(4) 1

(5) $-\infty$

(6) 1

(7) $\frac{\sqrt{2}}{2}$

(8) 1

(9) 0

(10) $-\infty$